

# Harmonic $G_2$ -structures on almost Abelian Lie groups

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## **Abstract**

Harmonic  $G_2$ -structures are critical points of the energy functional restricted to an isometric class. In this talk, we consider left invariant  $G_2$ -structures on 7-dimensional almost Abelian Lie groups and we propose a study between the 16-torsion classes and the harmonicity of a  $G_2$ -structure. For this, we characterise each torsion class of a  $G_2$ -structure in terms of the corresponding Lie algebra structure. And then, we provide the algebraic criteria on the Lie bracket, satisfying the harmonic condition  $\operatorname{div} T=0$ . Finally, this allows us to identify which torsion classes are harmonic. This talk is based on arXiv:2212.05168.